

**Labor Cost and Sugarcane Mechanization in Florida:
NPV and Real Options Approach**

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Introduction

The prospect of immigration reform has renewed growers' concerns of serious labor shortages and cost increases, given that a large percentage of the workforce is unauthorized for U.S. employment. Clearly, this is more of a concern for specialty crop agriculture that is highly labor intensive. In addition to the large labor requirements, labor use is often concentrated in a very short period, particularly at harvest time (Emerson 2007). This concern about labor-cost-increase seems quite legitimate if, as implied by the recent immigration reform proposals, only legal workers would be available for employers. This is because existing literature suggests significant wage gap between legal and illegal workers (Taylor 1992; Ise and Perloff 1995; Iwai et al. 2006).

There are several ways in which agricultural employers could deal with increased labor cost, but the most likely ones in the mid- to long-term would be the adoption of a technology with less labor use, and termination of current crop production if an alternative technology is not available (Emerson 2007). Mechanical harvesting is a typical example of the former option, whereas the latter option may involve changes to the cropping mix such that less labor is required, and possibly the mobility of capital for increased production in other countries.

The Florida citrus industry has been pursuing mechanical harvesting with an increased intensity over the past few years. Although there have been efforts to develop viable mechanical harvesters for citrus since the 1960s, the recent thrust has

resulted in a significant level of utilization of the continually evolving mechanical harvesters. Most of Florida oranges are dedicated to processing rather than the fresh market, an obvious advantage for mechanical harvesting. At the same time that there are continuing concerns about labor availability for harvest, the Florida citrus industry has faced difficulties from recent hurricanes to new diseases (citrus canker and citrus greening) to urban encroachment. The U.S. and Florida citrus industries are also facing increased international competition for citrus products. For example, the U.S. production of oranges fell by 29% between the 1980-81 and 2006-07 seasons while the Brazilian production of oranges doubled (USDA 1986, 2008). In addition, China has become a major citrus producing nation. They are second only to Brazil in total citrus production although over half of China's citrus production is tangerines and mandarin oranges.

As a result of all of these factors Florida citrus producers are searching for ways to better compete in the global marketplace. Mechanical harvesting has arisen as one of the possible ways that may improve their competitive position, particularly in light of potential labor disruptions due to labor availability and cost uncertainties. The estimated cost of mechanical harvesting and roadsiding of Florida oranges under typical conditions has a 25 cent per 90 pound box advantage relative to hand harvesting and roadsiding, roughly a 16% cost-savings (Roka). This is a significant cost difference, yet the adoption rate remains relatively low at about 7.5% of the acreage of Florida oranges in 2006-07 (UF).

Illustrative calculations with the 25 cent cost differential suggest a two year payback period for the investment that the grower would be required to make in

preparing the grove for mechanical harvesting. This also assumes that a third party is investing in the harvesting equipment, and that the \$1.35 per box cost is a sustainable rate by the harvesting company. The favorable cost situation for mechanical harvesting, yet hesitation by growers to adopt the new technology is not uncharacteristic of the experience in other commodities such as cotton, tomatoes, and sugar cane where mechanization has taken place in the past. This paper examines the Florida sugar cane mechanization experience with an alternative methodology as a prelude to evaluating the potential for mechanical harvesting adoption in citrus.

The large-scale mechanization of the Florida sugarcane harvest during the 1970s/80s serves as a historical example of how technologies evolved due to changes in local labor market conditions. Anecdotally, it is said that increases in labor cost forced sugarcane farmers to switch to mechanical harvesting.¹

Several studies of Florida sugarcane production have compared the cost and returns from mechanically harvested operations with those of hand cutting operations for the relevant period (Zepp and Clayton 1975, Zepp 1975). Based on data for the 1972-73 season, Zepp and Clayton (1975) found that the direct expenses (such as those for machinery and labor) were less per ton of cane when mechanical harvesting was used. However, these lower costs were more than offset by reduced revenue due to large field losses and higher trash content with mechanical harvesting, resulting in \$40.70 lower net returns per acre in comparison to hand-cut cane. If projected 1974-75 machinery operating rates had been used, the net returns per acre would have been

¹ Zepp (1975) reports that the average hourly wage of workers hired for sugarcane production and harvesting in Florida was 1.348 dollars for 1964-65 season, but it went up to 2.465 dollars for 1972-73 season for which period 15 percent of the Florida sugarcane crop was harvested mechanically.

about equal for the two harvesting methods, and the additional 10% labor cost increase would have been sufficient to overturn the net returns advantage (Zepp 1975).

Another important study on cost structure of Florida sugarcane farmers is Walker (1972) which estimates the production cost for all activities including harvesting for the model farmer, but does not distinguish the mode of harvesting.² However, a major problem with these previous studies is that they calculated and compared the cost and returns from two technologies for a single individual season, but did not analyze the dynamic decision-making process of farmers. There are two main approaches for that purpose: net present value (NPV) approach and real options approach (ROA).

The NPV approach simply assumes that the producer must invest if the NPV of the investment is greater than zero. In the case of Florida sugarcane, the farmer must switch to the mechanical harvesting if the discounted future cash flow less the investment cost for mechanical operation is higher than the discounted future cash flow (FCF) from the current operation. The ROA, which applies financial option theory for investment in real assets, assumes that the producer has the option to invest or wait, called “investment flexibility”. However, once the producer makes an irreversible investment, he exercises, or “kills” the option to invest and gives up the value of keeping the investment option alive. Hence the producer does not invest until the NPV of mechanical harvesting operation less the option value is greater than the NPV of hand cut operation (Dixit and Pindyck 1994, Trigeorgis 1996). The consideration for flexibility and irreversibility of investment in the real options approach often yields

² Zepp and Clayton (1975) use the cost estimate other than harvesting from Walker (1972), and use it as “production (growing) cost”.

much higher trigger value of the return (or cash flow) from mechanized harvesting operation than that calculated from NPV approach, delaying the investment decision until higher profit is more likely.³ Although we do not have preference over either method beforehand, the latter is supposed to yield more reasonable results.⁴ Since sugarcane farmers obviously have the ability to postpone their decision on investment, and, in general, investment in agriculture is at least partially irreversible (Napasintuwong and Emerson 2004),⁵ the consideration for these aspects of investment is important.

In the current study, we use these two methods to analyze the decision of the average sugarcane farmer in Florida as to mechanization of harvesting at the time of 1972-3 season. We also compute the adoption thresholds for the labor cost that triggered investment in mechanical harvesting for sugarcane in Florida. These methods also can incorporate another source of uncertainty which is said to be the other important factor causing the shift to mechanized harvesting: yield and price of sugarcane, and other costs than labor. We use these variables in our model.

There are several ways this study contributes to the literature of agricultural economics. First, although there are studies which use the real options approach for analysis of technology adoption in agriculture (Seo et al. 2006, Engel and Hyde 2003,

³ Real options approach can handle partially reversible investment decision. In our case this means that sugarcane farmer can turn back to hand cutting harvesting with some cost.

⁴ Some studies on technology adoption in agriculture support the validity of the ROA over the NPV approach (Seo et al. 2006, Engel and Hyde 2003, Carey and Zilberman 2002). These studies generally show that farmers would not invest in an alternative technology until the present value of investment exceeds the investment cost by a potentially large hurdle rate.

⁵ Napasintuwong and Emerson (2004) show that it is harder to substitute labor for capital when capital becomes expensive than it is to substitute capital for labor when labor becomes expensive.

Carey and Zilberman 2002), none focuses on the impact of labor market conditions on technology adoption. Given the current heated debate over proposed immigration reform, this is a crucial issue which should be analyzed. The current study analyzes the decision of the average sugarcane farmer in Florida as to mechanization of harvesting at the time of 1972-3 season, and computes the threshold value for labor costs which triggered the mechanical harvesting. Second, the current study builds the foundation for forecasting the possible effect of labor cost increases on the adoption of less labor-intensive operations. The study of the Florida sugarcane harvesting case helps us to forecast the timing and scale of adoption of mechanization for certain crops for which mechanized operation technology has already been developed (such as citrus).

Data

The most important source of data is cost for growing sugarcane from Walker (1972) and revenue and cost for harvesting sugarcane from Zepp and Clayton (1975). The second column of Table 1 shows activity-base cost for growing sugarcane for the model farm with 640 acres in total and 408 acres harvested in south Florida 1971-2 season, and the third column shows the forecasted value for each item provided by Walker (1972).

Table 1. Activity-base cost for growing sugarcane for the model farm with 640 acres in total and 408 acres harvested (\$ per 408 acres harvested)

Season	1971-2	1972-3
Land preparation	6,131.35	6,437.92
Planting	13,816.94	14,507.79
Cultivate plant cane	4,970.96	5,219.51
Cultivate stubble cane	8,480.96	8,905.01
Overhead expense	14,351.94	15,069.54
Overhead taxes	7,648.00	8,030.40
Cost of land	53,760.00	56,448.00
Total	109,160.15	114,618.16

Source: Walker (1972).

We convert the above table to cost-item base. The result is shown as Table 2.

Table 2. Cost for growing sugarcane for a model farm with 640 acres in total and 408 acres harvested (\$ per 408 acres harvested)

Season	1971-2	1972-3
Labor	11,352.66	11,920.29
Depreciation	7,044.24	7,396.45
Interest	4,514.51	4,740.24
Other costs	86,248.74	90,561.18
Total	109,160.15	114,618.16

Source: Authors calculated from Walker (1972).

The second column of Table 3 shows cost and revenue for harvesting sugarcane for a model farm with hand cut harvesting in south Florida 1971, and the third column shows those for mechanical harvesting farm.

Table 3. Revenue and cost for harvesting sugarcane for a model farm (\$ per gross ton).

	Hand cut harvesting	Mechanical harvesting
Season	1972-3	1972-3
Initial investment⁶	2.18	3.75
Annual machinery cost		
Depreciation	0.21	0.36
Repair and maintenance	0.23	0.59
Taxes, licenses and insurance	0.04	0.02
Fuel, oil and grease	0.06	0.19
Interest	0.10	0.16
Total machinery cost	0.64	1.34
Labor cost		
Cane cutter	2.41	0.00
Cutter or loader operator	0.02	0.38
Tractor driver	0.15	0.54
Dump operator	0.04	0.02
Ticket writer	0.02	0.01
Supervisor	0.07	0.12
Maintenance and repair	0.07	0.26
Scrapper	0.04	0.03
Utility man	0.02	0.00
Other	0.00	0.03
Total labor costs	2.85	1.39
Total annual cost	3.49	2.73
Revenue ⁷		
Sugarcane	10.88	10.46
Sugar payment	0.92	0.89
Molasses payment	0.36	0.36
Total revenue	12.16	11.70

Source: Zepp and Clayton (1975).

Next, we convert cost and revenue items in Table 3 into per net ton basis using net cane factor of 0.947 for hand cut harvesting and 0.893 for mechanical harvesting.⁸

Further we convert them into model farm bases with 640 acres in total and 408 acres

⁶ Initial investment cost happens only for season when it is made, although depreciation and interest payment happens annually.

⁷ Revenue items are recorded in per net ton basis. We converted them into per gross ton basis using net cane factor of 0.947 for hand cut harvesting and 0.893 for mechanical harvesting, both of which are presented by Zepp and Clayton (1975).

⁸ See Appendix B in Zepp and Clayton (1975) for the definition and calculation method for the net cane factor.

harvested after converting to per harvested acre basis by using net tons per acre of 38.35 for hand cut harvesting and 37.02 for mechanical harvesting.⁹ In Table 4 we show revenue and cost for growing and harvesting sugarcane for 72-5 seasons assuming that only labor and other harvesting cost for mechanical operation change as suggested by Zepp and Clayton (1975).¹⁰

Table 4. Revenue and cost for growing and harvesting sugarcane for a model farm (\$ per 408 acres harvested)

	Hand cut harvesting	Mechanical harvesting	Mechanical harvesting	Mechanical harvesting
Season	72-5	72-3	73-4	74-5
Revenue				
Sugarcane	190,597.20	176,896.56	176,896.56	176,896.56
Sugar payment	16,169.04	15,026.64	15,026.64	15,026.64
Molasses payment	6,238.32	6,022.08	6,022.08	6,022.08
Total revenue	213,004.56	197,945.28	197,945.28	197,945.28
Cost				
Growing				
Labor	11,920.29	11,920.29	11,920.29	11,920.29
Depreciation	7,396.45	7,396.45	7,396.45	7,396.45
Interest expenses	4,740.24	4,740.24	4,740.24	4,740.24
Other costs	90,561.18	90,561.18	90,561.18	90,561.18
Total	114,618.16	114,618.16	114,618.16	114,618.16
Harvesting				
Labor	47,095.44	23,863.92	17,767.27	11,670.63
Depreciation ¹¹	3,459.15	6,172.75	6,172.75	6,172.75
Interest expenses	1,588.31	2,788.27	2,788.27	2,788.27
Other costs	5,434.06	13,695.23	12,107.01	10,518.79
Total	57,576.96	46,520.16	38,835.29	31,150.43
Total cost	172,195.12	161,138.32	153,453.45	145,768.58
Return	40,809.44	36,806.96	44,491.83	52,176.70

Source: Authors calculated from Zepp and Clayton (1975).

⁹ We directly used per harvested acre basis for variables for which per harvested acre value is available instead of converting from per gross ton basis.

¹⁰ We use market data for all other items for 73-5 and all items including labor and other harvesting cost for further forecast, which is explained in the next section.

¹¹ Both Zepp and Clayton (1975) and Walker (1972) assume that depreciation and interest expenses are based on the initial investment value. Here we assume that the farmer is currently using hand cut harvesting so that depreciation and interest expenses are fixed on the current level for the hand cut harvesting, and they are fixed on the level of 72-3 season for the mechanical harvesting since we analyze the decision in that season.

Since Zepp and Clayton (1975) provide forecast of only labor and other cost for mechanical harvesting up to 1974-5 season, we need to use other sources for all other items in that period, and for all items after 1974-5 season. We use market data for time series of sugarcane yield, price, labor cost and other costs. We use the sugarcane yield and price data from the Florida *Field Crops Summary* (Florida Agricultural Statistics). The labor cost data are from unpublished U.S. Department of Labor administrative records; the other cost data is similarly from unpublished U.S. Department of Agriculture administrative records. We use the time series of sugarcane yield and price as long as possible but still in the relevant period: 1960-95. On the other hand, the time series of labor cost and other costs have many missing periods so that we use the following more restricted period to estimate the stochastic process: 1960-81.

Traditional NPV approach

In this section we analyze the mechanization decision by Florida sugarcane farmers using the NPV approach, which is the single, most widely used tool for large investments made by U.S. corporations (Copeland and Antikarov 2003). Although the implementation of the approach involves many steps, the basic concept of it is rather simple: the farmer would invest in mechanization if the discounted future free cash flow (FCF) forecasted for the mechanical-harvesting-operation less the investment cost is greater than that from the hand-cut-operation. Therefore, the first step of the approach is to estimate FCF for each operational mode for 1972-3 season using estimates from Zepp and Clayton (1975) and Walker (1972). Then, we model and estimate the stochastic process of sugarcane yield, price, labor cost and other costs and

run the Monte Carlo simulation to forecast FCF for the years after 1972. The forecasted FCF from each operation (the entity value) should be discounted at the opportunity cost of capital that is consistent with riskiness of these cash flows. We compute this discount rate which is called “Weighted Average Cost of Capital (WACC)”. The straightforward calculation of discounted free cash flow for each operational mode follows the above steps.¹²

Estimating FCF

The value of operation equals the discounted value of future FCF which is equal to the after-tax operating earnings of the farm, plus non-cash charges, less investments in operating working capital, property, and other assets (Copeland et al. 1994). This is the correct cash flow for this valuation model since it reflects the cash flow that is generated by a farm’s operation and available to all capital providers, both debt and equity.

We illustrate the calculation of the FCF for the model Florida sugarcane farmer with 640 acres in total and 408 acres harvested. Here we assume that there is no change in working operating capital since related information is unavailable for calculation.¹³ We calculate the FCF for 72-3 season from information in Table 4 which shows the revenue and cost for each operation mode. First, we calculate operating cash flow (operating CF) which is revenue minus labor cost and other costs. Second, we subtract depreciation from operating CF to have earnings before interest and taxes (EBIT). The FCF equals the EBIT minus taxes on EBIT, plus depreciation (since there is no actual

¹² This method called entity DCF model is mathematically equivalent to equity DCF model in which free cash flows to equity is discounted at the cost of equity.

¹³ Operating working capital equals operating current assets minus noninterest bearing current liabilities. Operating current assets include all current assets necessary for the operations of the business, including cash balances, trade accounts receivables, and inventories (Copeland et al. 1994).

cash outflow with depreciation), minus capital expenditures. The problem here is the tax rate on EBIT. Corporate tax data for 2004 indicates that agricultural production firms had net income of \$5.756 billion, income subject to tax was \$2.151 billion, and income tax prior to credits of \$0.646 billion, with credits of \$0.020 billion (Internal Revenue Service). This implies an average tax rate of 29% relative to taxable income. So we use 29% tax rate on EBIT. The calculation result for FCF for each year for each operation mode is given as Table 5.

Table 5. Estimated FCF from growing and harvesting sugarcane for the model farm (\$ per 404 acres harvested)

	Hand cut harvesting	Mechanical harvesting
Season	72-3	72-3
Revenue	213,004.56	197,945.28
Labor cost	59,015.73	35,784.21
Other costs	95,995.25	104,256.41
Operating CF	57,993.59	57,904.66
Depreciation	10,855.60	13,569.20
EBIT	47,137.99	44,335.46
Tax on EBIT (29%)	13,670.02	12,857.28
CAPEX	10,855.60	13,569.20
FCF	33,467.97	31,478.18

Forecasting beyond 72-3 season

Zepp and Clayton (1975) reported the explicit forecast for labor and other harvesting cost for mechanical operation for only two seasons from the 72-3 season, which forecasted that the former decreases by 17% and additional 21 % for respective season and the latter decreases by 1.5% for both seasons. Calculation of NPV and option value of the flexibility needs all other revenue and cost items for this period, and all items for longer period beyond two seasons which reflect the future cash flow process the farmers were facing at the decision time. A common approach often used in simulation

studies is the Monte Carlo simulation in which all stochastic series are generated for future periods using the estimated parameters and distributions of these series (Kobayashi 2003, Copeland and Antikarov 2003). Therefore, modeling and estimating the stochastic process for time series is a crucial step for the Monte Carlo simulation. Here we follow the approach suggested by Brockwell and Davis (1991, 2002). The first step suggested is creating a stationary process by transforming the time series of interest.¹⁴

We have four variables to forecast beyond the 72-3 season: yield, price, labor cost, and other costs. First, since all these variables are strictly positive we take the logarithm of these, and test the stationarity of these transformed series. Considering the possibility of drift and correlation between disturbance terms, we estimate the following formula using OLS for each variable for the augmented Dickey-Fuller test:

$$y_t = c + \gamma y_{t-1} + \sum_{p=1}^2 \gamma_p \Delta y_{t-p}.$$

With this estimation we test $\gamma = 1$. Also note that we use $p = 2$ since none of the differences lagged more than two times are statistically significant for the four estimations. Table 6 shows the estimates and standard errors for the four series. The test statistic for the ADF test for each series is given as $(\hat{\gamma} - 1) / SE(\hat{\gamma})$.

¹⁴ A simple example is producing a random variable from a series which follows the geometric Brownian motion with trend. Taking the first difference of logarithm of the series and subtracting the mean of the first difference yields a stationary random series.

Table 6. Estimated coefficients, standard errors, and ADF test statistics

	Yield	Price	Labor cost	Other costs
c	3.49 (1.15)	0.35 (0.23)	-0.10 (0.34)	-1.18 (0.98)
γ	-0.0045 (0.33)	0.90 (0.08)	1.05 (0.09)	1.15 (0.11)
γ_1	-0.0051 (0.25)	0.12 (0.16)	-0.28 (0.25)	-0.55 (0.27)
γ_2	-0.18 (0.18)	-0.44 (0.16)	-0.43 (0.24)	-0.47 (0.28)
Observations	33	33	19	19
ADF test	-3.03	-1.32	0.56	1.34

Since the critical value with 5 % level of significance is approximately -3.00 for 19 observations, and -2.97 for 33 observations, we can barely reject the null hypothesis of a unit root for the log of yield, but cannot reject the null hypothesis for all others. Then we take the first difference of each series and repeat the same test procedure for the transformed data.¹⁵ The results are shown in Table 7. The test results show that the first difference is enough to produce the stationary process from each series. We further subtract the sample mean of the transformed series from the transformed series.

Table 7. Estimated coefficients, standard errors, and ADF test statistics after taking the first difference

	Yield	Price	Labor cost	Other costs
c	0.00 (0.01)	0.053 (0.041)	0.09 (0.04)	0.13 (0.05)
γ	-1.18 (0.25)	-0.40 (0.22)	-0.62 (0.35)	-0.65 (0.39)
γ_1	0.54 (0.15)	0.48 (0.16)	0.39 (0.23)	0.27 (0.24)
No. of observation	33	33	19	19
ADF test	-8.63	-6.37	-4.66	-4.24

The next step is to model the generated residuals obtained by differencing the series and subtracting the sample mean of the difference. If there is no dependence

¹⁵ We use $p=1$ since the only statistically significant lagged difference is the first one.

among these residuals, we can regard them as observations of independent random variables. However, if there is significant dependence among the residuals, we need to look for a more complex stationary time series model to account for the dependence. This will be to our advantage since dependence means that past observations of the residual sequence can assist in predicting future values. Here we implement some tests for the hypothesis that the residuals generated above are observations of independent and identically distributed (iid) random variables. In Table 8, we show the test results from the following five tests of randomness: Ljung–Box, McLeod-Li, Turning point, Difference-sign, and Rank test. Since the randomness is not rejected by any of the five tests at the 5% level of significance, we do not need to use the theory of stationary processes to find a more appropriate model.

Table 8. Tests of randomness

Variable	Test	Test statistics	Test distribution ¹⁶	p-value
Yield				
	Ljung – Box	21.29	Chi-Square (20)	0.38
	McLeod – Li	20.82	Chi-Square (20)	0.41
	Turning point	19	AN(22.00, 2.43)	0.22
	Difference-sign	17	AN(17.00, 1.73)	1.00
	Rank	0.00	AN(0.00, 35.21)	0.62
Price				
	Ljung - Box	15.69	Chi-Square (20)	0.74
	McLeod - Li	21.29	Chi-Square (20)	0.38
	Turning points	21	AN(22.00, 2.43)	0.68
	Difference-sign	16	AN(17.00, 1.73)	0.56
	Rank	0.00	AN(0.00, 35.21)	0.18
Labor cost				
	Ljung - Box	16.78	Chi-Square (15)	0.33
	McLeod - Li	7.04	Chi-Square (15)	0.96
	Turning points	11	AN(12.67, 1.85)	0.37
	Difference-sign	9	AN(10.00, 1.35)	0.46
	Rank	0.00	AN(0.00, 16.56)	0.81
Other costs				
	Ljung - Box	12.86	Chi-Square (15)	0.61
	McLeod - Li	11.12	Chi-Square (15)	0.74
	Turning points	16	AN(12.67, 1.85)	0.07
	Difference-sign	11	AN(10.00, 1.35)	0.46
	Rank	0.00	AN(0.00, 16.56)	0.63

However, further consideration is needed about the potential interdependence between residuals. That is, multivariate time series $\{X_t\}$ may have not only serial dependence within each component series but also interdependence between the different component series $\{X_{it}\}$ and $\{X_{jt}\}$, $t \neq s$, $i \neq j$. In the current case, the interdependence between cost series and between yield and price is tested because of the mismatch in the number of observations. The second-order properties of the

¹⁶ AN() stands for approximately normal distribution.

multivariate time series $\{X_t\}$ are specified by the mean vector $\boldsymbol{\mu}_t = \begin{bmatrix} \mu_{t1} \\ \mu_{t2} \end{bmatrix}$ and covariance matrix

$$\boldsymbol{\Gamma}(t+h,t) = \begin{bmatrix} \gamma_{11}(t+h,t) & \gamma_{12}(t+h,t) \\ \gamma_{21}(t+h,t) & \gamma_{22}(t+h,t) \end{bmatrix},$$

where $\gamma_{ij}(t+h,t) = \text{cov}(X_{t+h,i}, X_{t,j})$, but $\gamma_{ij}(t+h,t) = \gamma_{ij}(h)$ for stationary series so that $\boldsymbol{\Gamma}(t+h,t) = \boldsymbol{\Gamma}(h)$ and $\boldsymbol{\mu}_t = \boldsymbol{\mu}$. Since the random white noise assumption is not rejected by the test of randomness for the all four transformed series, we can use the following statistics for the test of independence between the two sets of two series: $\hat{\rho}_{ij}(h) = \hat{\gamma}_{ij}(h) / \sqrt{\hat{\gamma}_{ii}(0)\hat{\gamma}_{jj}(0)}$. An approximate test for independence can be obtained by comparing the values of $|\hat{\rho}_{12}(h)|$ with $1.96n^{-0.5}$ for 5% level of significance where n is number of observations (Brockwell and Davis 2002). Table 9 shows the test result for h up to 3 which implies that the independence hypothesis is rejected for yield and price.

Table 9. Tests of independence between yield and price, and between costs

	$\hat{\rho}_{12}(0)$	$\hat{\rho}_{12}(1)$	$\hat{\rho}_{12}(2)$	$\hat{\rho}_{12}(3)$	Critical value
Yield and price	-0.38	0.089	0.30	-0.30	0.35
Labor and other costs	-0.014	0.28	0.025	0.070	0.48

Since the test of independence is rejected for the former, we need to model for interdependence between the series. Here we assume that the two sets of vector series have the following multivariate AR(p) process given as.¹⁷

$$X_t = \boldsymbol{\varphi}_0 + \boldsymbol{\Phi}_1 X_{t-1} + \dots + \boldsymbol{\Phi}_p X_{t-p} + U_t, \{U_t\} \sim \text{WN}(\mathbf{0}, \boldsymbol{\Sigma})$$

where WN stands for white noise process. From the above equation we can show that

¹⁷ Multivariate ARMA(p, q) model supports more general structure. However, it is not always possible to distinguish between multivariate ARMA models of different orders. Here we focus on the AR process to avoid the identification problem.

$$\underline{\Sigma} = \Gamma(0) - \sum_{j=1}^p \Phi_p \Gamma(-j) \text{ and } \Gamma(i) = \sum_{j=1}^p \Phi_p \Gamma(i-j), \quad i=1,2,\dots,p, \text{ where } \Gamma(\cdot) \text{ is the covariance}$$

matrix defined before.¹⁸ For each value of i and j , we have sample covariance so that we can calculate Φ_p and $\underline{\Sigma}$ from the above two equations for a given p . Further we search for the optimal p that minimizes the bias-corrected version of the Akaike Information Criteria referred to as the AICC (Brockwell and Davis 2002):

$$\text{AICC} = -2\ln L(\Phi_1, \dots, \Phi_p, \underline{\Sigma}) + 2(pm^2 + 1)nm/[nm - pm^2 - 2],$$

$$\text{where } L(\Phi_1, \dots, \Phi_p, \underline{\Sigma}) = (2\pi)^{-nm/2} \left\{ \prod_{j=1}^n \det \underline{\Sigma} \right\}^{-1/2} \exp \left\{ -\frac{1}{2} \sum_{j=1}^n U_j' \underline{\Sigma} U_j^{-1} \right\} \text{ and } U_j = \mathbf{X}_j - \hat{\mathbf{X}}_j,$$

and m is number of variables in the vector which is 2 in our case. The likelihood function assumes the bivariate normal distribution for white noise process.¹⁹ We have the following estimation result for between yield and price,

$$\begin{bmatrix} X_{t1} \\ X_{t2} \end{bmatrix} = \begin{bmatrix} 0.00 \\ 0.00 \end{bmatrix} + \begin{bmatrix} -0.66 & -0.077 \\ 0.67 & 0.17 \end{bmatrix} \begin{bmatrix} X_{t-1,1} \\ X_{t-1,2} \end{bmatrix} + \begin{bmatrix} -0.45 & 0.077 \\ 0.60 & -0.40 \end{bmatrix} \begin{bmatrix} X_{t-2,1} \\ X_{t-2,2} \end{bmatrix} + \begin{bmatrix} U_{t1} \\ U_{t2} \end{bmatrix}$$

$$\text{where } \begin{bmatrix} U_{t1} \\ U_{t2} \end{bmatrix} \sim WN \left(\begin{bmatrix} 0 \\ 0 \end{bmatrix}, \begin{bmatrix} 0.0054 & -0.0021 \\ -0.0021 & 0.042 \end{bmatrix} \right) \text{ and AICC} = -74.55,$$

and between labor and other costs,

$$\begin{bmatrix} X_{t1} \\ X_{t2} \end{bmatrix} = \begin{bmatrix} 0.00 \\ 0.00 \end{bmatrix} + \begin{bmatrix} U_{t1} \\ U_{t2} \end{bmatrix}$$

$$\text{where } \begin{bmatrix} U_{t1} \\ U_{t2} \end{bmatrix} \sim WN \left(\begin{bmatrix} 0 \\ 0 \end{bmatrix}, \begin{bmatrix} 0.020 & -0.00052 \\ -0.00052 & 0.027 \end{bmatrix} \right) \text{ and AICC} = -38.65.$$

¹⁸ Also we have $\mu = (I - \Phi_1 - \dots - \Phi_p)^{-1} \phi_0$.

¹⁹ Shapiro-Wilk W test does not reject the normality for all four residual series at 5% level of significance.

Using the above estimated model we can generate sample future pass for each variable. For the first year after the observed period, which we call $n+1$, the vector X_{n+1} is estimated as $\hat{X}_{n+1} = \hat{\mu} + \hat{\phi}_1 X_n + \hat{\phi}_2 X_{n-1}$ which depends on the estimated coefficients and past values of the series. Then we can have a realized value of X_{t+1} by adding on the right hand side a randomly generated white noise U_{t+1} which we assume follows bivariate normal distribution with covariance matrix given as the estimation result. Since X_{t+1} is the change in the de-trended (mean-subtracted) log of the original series, we can generate a sample of the original series by adding the trend, taking exponential and multiply it to the previous value.²⁰ In the same way we can generate a sample value for period $t+2$ using the generated sample of $t+1$ and newly generated white noise U_{t+2} . Repetition of these steps nine times for each vector will yield one sample of future nine-year pass for each variable. We generate 100,000 sets of the future pass for four variables with which we calculate 100,000 sets of nine-year future FCF pass for each operation mode. The average of generated FCF for each year and expected annual growth rate of FCF for each operation mode is given as Table 10.

Table 10. Forecasted FCF from growing and harvesting sugarcane after 72-3 season (\$)

	73-4	74-5	75-6	76-7	77-8
Hand cut	32,880.05	32,882.90	25,847.06	20,299.64	20,848.51
Mechanical	36,505.76	42,991.52	37,478.13	33,386.73	35,036.43
	78-9	79-80	80-1	81-2	
Hand cut	17,011.08	9,449.28	4,457.93	-470.85	
Mechanical	32,698.77	26,970.87	23,726.29	20,617.16	

²⁰ Since Walker (1972) indicates that about one third of other costs for production belong to variable cost, we assume one third of total other costs are variable. Also, Zepp and Clayton (1975) show that about 88 % of revenue is from direct sale of sugarcane. Considering other government program and insurance purchase, we assume that 50% of market volatility is transferred to farmers (5% loss of revenue when the market value implies 10% revenue loss).

From Tables 5 and 10 we calculate the expected growth rate of FCF for each mode: -21.59% for hand cut harvesting, and -4.45% for mechanical harvesting operation.²¹

Weighted Average Cost of Capital

Now that we have estimated future free (entity) cash flows, the next step is to discount the FCF by the appropriate discount rate. The discount rate we use is the weighted average cost of capital (WACC) which is the time value of money used to convert the expected FCF into a present value for all investors. Since entity cash flows are available for payment to both sources of capital, debt and equity, the discount rate must comprise a weighted average of the marginal costs of both sources of capital. In our application WACC is given by

$$WACC = k_b(1-T)\frac{B}{B+S} + k_s\frac{S}{B+S},$$

where k_b is the pretax market expected yield to maturity on debt, T is the marginal tax rate for the entity, which is 29% in our application, B is the market value of interest-bearing debt, and S is the market value of equity, and k_s is the market-determined opportunity cost of equity capital. We take $k_b=8\%$ directly from Zepp and Clayton (1975), and Walker (1972). We calculated the debt to asset ratio for the fruitful rim for “other field crops” (includes sugar) averaged for the years 1996-2005 (ARMS). The result is 0.12 so that we estimate $B/(B+S)=0.12$, and $S/(B+S)=0.88$.²²

²¹ Growth rate is calculated using mean FCF for 81-2 season and that for 72-3 season. However, since the expected FCF for 81-2 season is negative for the hand cut operation, the growth rate for it is calculated using mean FCF for 80-1 season and that for 72-3 season.

²² There are many other approaches to estimate the market value of equity. Especially, Copeland et al. (1994) suggests iteration method to deal with the circularity problem involved in estimating WACC and the market value of equity. However, we simply use the market average debt/asset ratio, since the necessary information is not available to implement the more involved method for our case study.

Finally we estimate k_s , the market-determined opportunity cost of equity capital. Here we use the most widely used estimation method: capital asset pricing model (CAPM). The equation for the cost of equity from the CAPM is given as

$$k_s = r_f + [E(r_m) - r_f] \beta_j,$$

where r_f is the risk-free rate of return, $E(r_m)$ is the expected rate of return on the overall market portfolio, so that $[E(r_m) - r_f]$ is the market risk premium. β_j is the systematic risk of the equity which is defined as $COV(r_j, r_m)/VAR(r_m)$ where r_j is the rate of return from the equity to be evaluated. We calculated geometric average of annual rate of return from Treasury bills for years 1960-95, and use it for the risk-free rate of return ($r_f = 6.11\%$). We also calculated geometric average of annual rate of return from stock using S&P 500 for the same period, and use it for the overall market portfolio ($E(r_m) = 10.67\%$ and the risk premium = 4.55%).²³ We use the industry beta for food and kindred products of 1.04 from Copeland et al. (1994), because this is the industry with risk closest to the sugar industry. Using these figures we estimate for the WACC approximately 10.23%.

NPV calculation

PV for year t is given as $PV_t = \sum_{\tau=t+1}^{1982} \frac{E(FCF_{\tau})}{(1+WACC)^{\tau-t}} + \frac{(1+g)FCF_{1982}}{(1+WACC)^{1982-t}(WACC-g)}$ for

$t < 1982$. $PV_{1982} = \frac{(1+g)FCF_{1982}}{(WACC-g)}$. The latter is continuing value after the explicit

forecast period estimated using growing FCF perpetuity formula in which g is the expected growth rate in FCF in perpetuity (-21.59% for hand cut harvesting, and

²³ We calculated from dataset provided by Damodaran which is available at <http://pages.stern.nyu.edu/~adamodar/pc/datasets/histretSP.xls>.

-4.45% for mechanical harvesting operation).²⁴ NPV for year t simply adds FCF of that year to PV: $NPV_t = FCF_t + PV_t$ ($-I_t$ if the investment is made in that year). We also calculate FCF as percentage of NPV for each year to be used for ROA later. In Table 11 we show sample mean of these figures from the generated 100,000 samples.

Table 11. PV and NPV from growing and harvesting sugarcane with each mode of operation (\$)

Season	72-3	73-4	74-5	75-6	76-7
PV from hand cut	147,545.90	129,759.79	110,151.32	95,572.73	85,050.18
NPV from hand cut	181,013.87	162,639.84	143,034.22	121,419.80	105,349.83
FCF as % of NPV	18.49%	20.22%	22.99%	21.29%	19.27%
PV from mechanical	288,337.22	281,328.35	267,116.72	256,964.63	249,865.39
NPV from mechanical harvesting	319,815.40	317,834.11	310,108.24	294,442.76	283,252.11
FCF as % of NPV	9.84%	11.49%	13.86%	12.73%	11.79%
Season	77-8	78-9	79-80	80-1	81-2
PV from hand cut	72,902.30	63,349.13	60,380.47	62,099.45	68,923.07
NPV from hand cut	93,750.82	80,360.21	69,829.75	66,557.39	68,452.23
FCF as % of NPV	22.24%	21.17%	13.53%	6.70%	-0.69%
PV from mechanical	240,390.18	232,283.33	229,075.05	228,783.14	231,570.49
NPV from mechanical	275,426.62	264,982.10	256,045.91	252,509.43	252,187.65
FCF as % of NPV	12.72%	12.34%	10.53%	9.40%	8.18%

In Table 12 we pick up the NPV and initial investment cost in 1972-3 season to show the decision of the model farmer as to mechanizing harvesting at that time using the traditional NPV approach.

Table 12. NPV and initial investment cost for each operation for 1972-3 season (\$)

	NPV	Initial investment cost	NPV – inv. cost
Hand cut harvesting	181,013.87		181,013.87
Mechanical harvesting	319,815.40	63,431.21	256,384.19

²⁴ Changing the assumption that the farmer continues to hold the operation after 81-2 season does not affect the value of PV, but the summation is taken over infinite future. Also, since g is negative, the continuing value is set zero if the FCF in 1982 is negative. It is not plausible that an agent continue to hold an asset with negative value which will continuously lose the value.

Since NPV less initial investment cost of mechanization is more than NPV for operation with hand cut harvesting, the traditional NPV approach suggests that the model farmer should have switched to mechanized operation even in 72-3 season. We can see this from the data: negative growth rate of FCF (-22.27 %) and relatively high FCF/PV ratio (over 18%), that is, growing and harvesting with hand cut operation generates relatively high FCF, but its expected growth is negative in the future. In comparison the FCF of mechanized operation has relatively higher growth rate (-4.59%). But, remember that only 15% of sugarcane was mechanically harvested at that time (much of which was experimental) and most farmers delayed mechanization until mid- and late 1980s (Figure 1). The traditional NPV approach cannot explain why Florida sugarcane farmers had not made the investment for mechanization in the early 1970s.

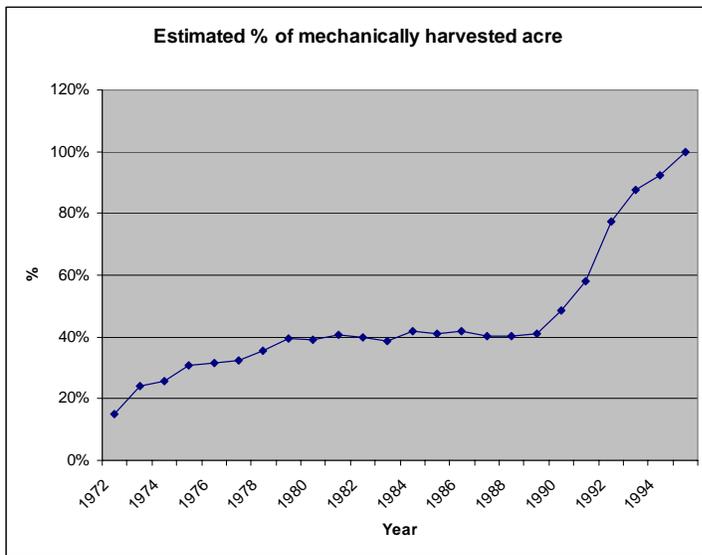


Figure 1. Estimated percentage of mechanically harvested acre²⁵

²⁵ We estimate % of mechanically harvested acre from number of H-2A workers (USDL, Annual Reports) by the following formula: $1 - 0.85 * I_t / I_{1972}$ where $I_t = (\text{H-2A workers for season } t) / (\text{total harvested acre for season } t)$.

Real Options Approach

The traditional NPV approach simply assumes that the farmer must switch to the mechanical harvesting if the NPV less the investment cost for mechanization is higher than the NPV from the current operation. The analysis in the previous section suggests that, based on the NPV approach, farmers should have already switched to mechanical harvesting in 1972-3 season. However, only 15% of sugarcane was mechanically harvested at that time and most farmers delayed mechanization until mid- and late 1980s; the NPV approach cannot offer an explanation for this delay. The real options approach (ROA), which applies financial option theory for investment in real assets, assumes that the producer has the option to invest or wait, called “investment flexibility”. However, once the producer makes an irreversible investment, he exercises the option to invest and gives up the option value of investment. Hence the producer does not invest until the NPV less investment cost is greater than the NPV for the current operation by the margin of the option value of investment. Therefore calculating the option value of investment is the most important part of the ROA.

One problem with applying the ROA in our case study is that there are four sources of uncertainty, sugarcane yield, price, labor cost and other costs which make it difficult solving the problem analytically. However, a numerical solution of the problem with more than two separate sources of uncertainty is not common either (using method such as lattice solver and finite difference method). The most common approach for the case of many sources of uncertainty is the consolidated approach suggested by Copeland and Antikarov (2003). The consolidated approach, a very widely used approach in real business applications, combines many uncertainties into one through the Monte Carlo simulation. The approach is based on the following

theorem attributable to Samuelson (1965): regardless of the pattern of cash flows expected in the future, the changes in the present value will follow a random process so that return is iid process, as long as investors have rational expectations about the cash flow. The assumption made for this theorem is quite general: all the information about the expected future cash flows is already backed into the current PV in such a way that, if expectations are met, investors will earn exactly their expected cost of capital. We assume that this assumption is met for our case study.²⁶

Another question is how far forward to extend the horizon for our application. Copeland and Antikarov (2003) note that “*the present value of their expected cash flows that are reasonably far out in time, is discounted by a present value factor rapidly diminishes toward zero.*” and conclude “*A rule of thumb worth considering is to ignore options beyond about 15 years out.*” (p. 239).²⁷ Considering the changing business environment including the technology of harvesting and production, we assume that the current option is available for farmers for 10 years.

Methodology to calculate the value of option to invest

Here we show the formula to calculate the option value of mechanization investment for the farmer. After harvesting in year $t \in [0, T]$ a farmer has two options in the action set: $a_t = \{0, 1\}$ where 0 if he does not invest, 1 if he invests. The feasible control set is that the farmer can exercise the investment option one time in $t \in [0, T]$. Given the action in this year, the cash flow function for the next year is given as,

$$f(t+1|a_t, FCF_t) = \begin{cases} FCF_{t+1} & \text{if } a_t = 0, \\ NPV_{t+1}^{mech} - I_t & \text{if } a_t = 1, \end{cases}$$

²⁶ See Copeland et al. (2003) for empirical evidence supporting Samuelson’s theorem.

²⁷ Our calculation of option value also shows that including cash flows after 11 years from the current year makes negligible change in the value.

NPV_{t+1}^{mech} is the net present value of cash flow from year $t+1$ from the mechanized operation. After exercising the investment option, the cash flow becomes zero.²⁸ The farmer's objective function is given as

$$V^C(FCF_0) = \tilde{E} \left[\sum_{t=0}^T \frac{f(t+1|a_t, FCF_t^C)}{(1+r_f)^{t+1}} \right],$$

where FCF_t^C is the FCF in year t given the actions up to year t , \tilde{E} is the expectation operator with the risk neutral probability which is the martingale measure of the uncertain cash flow (Kijima 1994). The farmer chooses the control among the feasible control set $C_a(FCF_0)$ to maximize the objective function so that,

$$V(FCF_0) = \max_{C \in C_a(FCF_0)} V^C(FCF_0).$$

Note that the above $V(FCF_0)$ is the net present value of the manual operation plus the option value of mechanization investment when the optimum control is taken. The Bellman equations of the optimization problems are given as

$$\begin{aligned} J_T(FCF_T) &= \max[NPV_{T+1}/(1+WACC), NPV_{T+1}^{mech}/(1+WACC) - I_T], \\ J_t(FCF_t) &= \max[\tilde{E}_t \left(\frac{J_{t+1}(FCF_{t+1})}{1+r_f} \right), NPV_{t+1}^{mech}/(1+WACC) - I_t]. \end{aligned}$$

Note that NPV_{t+1}^{mech} and NPV_{T+1}^{mech} include the perpetuity value of each operation.

Solving the above equations iteratively results in $V(FCF_0)$, which is the value of the objective function resulting from the optimum control. In the following sections, we follow the above method and calculate the NPV of the manual operation and the option value of mechanization investment.

²⁸ Actually there is cash flow from mechanized operation, but they are included in NPV_{t+1}^{mech} . This is made just for calculation convenience, but the result is the same.

Monte Carlo simulation to combine uncertainties

The regular first step for the consolidated approach is to model and estimate the stochastic process for the sources of uncertainty, the four time series in our case. Next we use these estimates to generate sample future pass for each variable, and calculate sample future pass for FCF. We have already taken these steps in the NPV section and generated 100,000 sets of nine-year future pass of FCF. We use the generated sample FCF to calculate the standard deviation of the annual rate of return from operation with hand cut harvesting.

The annual rate of return is defined as $z = \frac{FCF_1 + PV_1}{PV_0} - 1$. We use the present value for 72-3 season as PV_0 , which is fixed at \$150,214.52 (Table 11), and the FCF and present value for 73-4 season as FCF_1 and PV_1 . Therefore we have 100,000 samples of annual returns from which the average and standard deviation are calculated as 0.1023 and 1.7734 respectively. The former is very close to the WACC as expected, and the latter indicates a highly volatile rate of return from the sugarcane farming with hand cut harvesting. The theory of ROA generally predicts that higher volatility results in a high value of keeping the option alive which gives the investor an incentive to further delay the investment, since the volatility raises the value of waiting to see what is going to happen in the future (Dixit and Pindyck 1994). This high volatility of returns and resulting high value of the option may be enough to overturn the conclusion from the NPV approach, that is, the farmer should have already switched to mechanized operation in 72-3 season.

Option value computation

In this section we calculate option value of the mechanization investment for the Florida sugarcane farmer. First we build the binomial tree which approximates the transition of PV. For illustration purposes we show the PV binomial tree for the first three years.

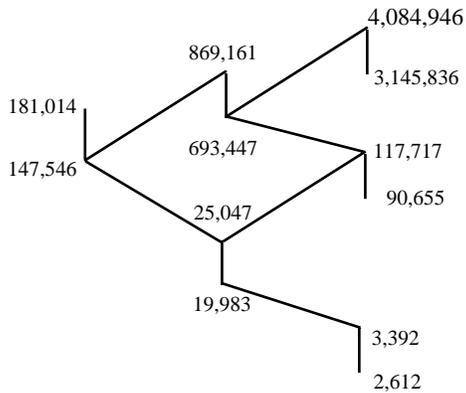


Figure 2. PV binomial tree for the first three years

The first figure, \$181,014, is the NPV_{1972} for the hand cut operation calculated using NPV approach (Table 11). In order to subtract FCF_{1972} we multiply it by $(1-0.1849)$ where 18.49% is FCF_{1972} as percentage of NPV_{1972} shown in Table 11. Then we have $PV_{1972}=\$147,546$. Since the estimated annual volatility for the current operation is 1.7734, the NPV1 would be either \$869,161 ($PV_{1972} \exp(1.7734\sqrt{dt})$) or \$25,047 ($PV_{1972} \exp(-1.7734\sqrt{dt})$) where $dt=1$. After subtracting the FCF_{1973} using FCF percentage of 20.22% for season 1973, we have the PV_{1972} for each state: \$693,447 and \$19,983. We continue this calculation up to 1981-2 season.

The final step of the analysis is real options calculations using the PV event tree built above. Real options calculations compute the present value of the sugarcane production with hand cut harvesting with option to make or postpone the investment

(investment flexibility). Unlike the event tree, real options calculations start at the end of the tree, the season the option expires. To illustrate, we show the calculation using only three nodes in the final season ($t=1981$) and one year before ($t=1980$). We pick up the following three nodes involving the $t=1981$, 1980 from the PV event tree.

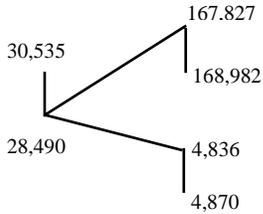


Figure 3. Part of PV binomial tree for the final two years

The decision in the final year is fairly simple: compare the PV_{1981} from the current operation and that from the mechanized operation less investment cost. The lower node of the final year has PV_{1981} of \$4,870 which is lower than that from the mechanized operation less the investment cost: $\$141,631 = \$231,570 - \$89,939$ so that the farmer switches to the mechanized operation.²⁹ On the other hand, the PV_{1981} in the upper node, \$168,982 is greater than \$141,631 so that the farmer does not switch to mechanization. We then put in the PV_{1981} with flexibility option of \$141,631 and \$168,982 in lower and upper node in the real options calculation tree below (Figure 4). As usual, we add the FCF in the final year with FCF percentage of -0.04% for 1981 season yielding NPV_{1981} with flexibility option of \$141,598 and \$167,827 in each node.

²⁹ PV_{1982}^{mech} of \$129,412 is from Table 11. Investment cost increases 3.956 % annually according to the estimation from Zepp and Clayton (1975) so that $InvCost_{1981} = 63,431.21 * (1 + 0.03956)^9 = 89,939$.

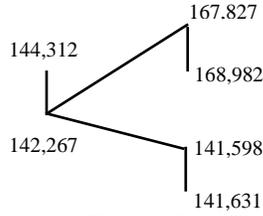


Figure 4. Part of real options calculation tree for the final two years

The calculation of value of the current operation with investment option for 1980 can be done by two approaches which are proven to be mathematically equivalent: risk neutral probability approach and replicating portfolio approach. Here we explain the former approach. Suppose that the farmer creates a hedge portfolio composed of one share of the current operation and a short position of m units of the investment option and the current operation.³⁰ So-called hedge ratio m is chosen so that the portfolio is risk free in the next period. Then the following condition must be true for the next period:

$$e^{\sigma} PV_{1980} - mC_{1981}^u = e^{-\sigma} PV_{1980} - mC_{1981}^d$$

where C_{1981}^u is the value of investment option and the current operation in the “UP” state in 1981, C_{1981}^d is that in the “DOWN” state. Solving this yields

$$m = \frac{(e^{\sigma} - e^{-\sigma})PV_{1980}}{C_{1981}^u - C_{1981}^d}. \text{ Since the hedge portfolio is risk free in the sense that the value}$$

of it is same regardless of the state of the next period, the non-arbitrage principle requires that the farmer has to earn the risk free rate r_f from this portfolio. This

³⁰ Here we assume that sugarcane farming is marketable in any unit. If this assumption is not true, we need to assume one of alternative assumptions: there is the twin security which is perfectly correlated with FCF of his operation, or the PV of the project without flexibility (i.e. the traditional NPV) is the best unbiased estimate of the market value of the project with flexibility option. The latter assumption is called the Marketed Asset Disclaimer (MAD) (Copeland and Antikarov 2003).

means that the value of holding current operation and investment option (denoted C_{1980}) must satisfy the following condition:

$$(PV_{1980} - mC_{1980})(1 + r_f) = e^\sigma PV_{1980} - mC_{1981}^u = e^{-\sigma} PV_{1980} - mC_{1981}^d.$$

Solving for C_{1980} after substituting $m = \frac{(e^\sigma - e^{-\sigma})PV_{1980}}{C_{1981}^u - C_{1981}^d}$ yields

$$C_{1980} = [qC_{1981}^u + (1 - q)C_{1981}^d][1 + r_f]^{-1}.$$

where $q = \frac{(1 + r_f) - e^{-\sigma}}{e^\sigma - e^{-\sigma}}$ is called risk neutral probability since the value of the current operation with option value is the expectation based on q , discounted by risk free rate (Tavella 2002). Simply substituting $C_{1981}^u = 167,827$ for the up state and $C_{1981}^d = 141,598$ for the down state from Figure 4; and r_f is risk free rate of return, 0.0611; and sigma = 1.7734, yields $C_{1980} = \$137,296$

Next we compare this holding value and PV for mechanized operation less investment cost, which yields PV_{1980} with option value: PV_{1980} with option value = $\text{Max}[\$137,296, \$228,783 - \$86,516] = \$142,267$. This means the farmer exercise the investment option for this particular node. As usual we add FCF_{1980} yielding the NPV_{1980} with investment option of $\$144,312$ for this node. We repeat these steps for other nodes of season 81-2 and 80-1, and up to season 72-3, and compute the NPV_{1972} with option value = $\$357,179$.

Then the option value is simply calculated as: (NPV_{1972} with option value) - $NPV_{1972} = \$357,179 - \$181,014 = \$176,166 = \text{OptValue}_{1972}$ ³¹ which is the value of option to make or postpone the investment (investment flexibility). Since making

³¹ More precisely $\$357,179.45 - \$181,013.87 = \$176,165.58$.

investment at that time means exercising the option to invest, the farmer loses the option value of flexibility at the same time. The farmer would not make an investment until it is profitable enough to overcome the loss of option value to wait. Therefore the decision rule of investment for the farmer is “invest if NPV of mechanized operation less investment cost and option value is greater than NPV of the current operation”. The calculation is given as: $NPV_{1972}^{mech} - InvCost_{1972} - OptValue_{1972} = \$319,815 - \$63,431 - \$176,166 = \$80,219 < \$181,014 = NPV_{1972}$,³² which suggests that the farmer should not invest in the mechanization in 1972-3 season. We summarize these results as Table 13.

Table 13. NPV and initial investment cost for each operation for 1972-3 season (\$)

	NPV	Initial investment cost	Option Value	NPV-Inv Cost-Option Value
Hand cut harvesting	181,013.87			181,013.87
Mechanical harvesting	319,815.40	63,431.21	176,165.58	80,218.60

Finally we compute the threshold value of the current labor cost that makes the farmer indifferent between mechanization and the current options so that $NPV_{1972}^{mech} - InvCost_{1972} - OptValue_{1972} = NPV_{1972}$. Note that the current labor cost increase is the level effect in the sense that it yields the same percentage labor cost increase from the actual level in subsequent periods without changing the transition. The resulting values including the threshold labor cost (52.76% increase from the actual labor cost) are given as Table 14.

³² $\$319,815.40 - \$63,431.21 - \$176,165.58 = \$80,218.60 < \$181,013.87$.

Table 14. NPV Threshold labor cost and resulting NPV and option value for 1972-3 season (\$)

	Labor cost	Resulting NPV	Initial investment cost	Resulting Option value	NPV -Inv Cost -Option value
Hand cut harvesting	90,152.43 (52.76% increase)	-14,608.28			-14,608.28
Mechanical harvesting	54,663.96 (52.76% increase)	181,107.56	63,431.21	132,284.63	-14,608.28

The conclusion from the ROA is that the farmer must not switch to mechanized operation in 72-3 season, which is the exact opposite conclusion to that suggested by the traditional NPV approach. Since the sugarcane farmers in Florida are exposed to highly volatile FCF, the value of keeping the flexibility option alive is very high, enough to overturn the conclusion from the traditional NPV approach. As the theory of ROA shows, high volatility of FCF gives the investors incentive to wait until the uncertainty resolves. The ROA correctly predicts that average farmers would not have invested in mechanization in 72-3 season. Threshold level analysis shows, for the immediate investment, it takes more than 52% increase in the labor cost for both operations. This indicates that there was a rather large margin between the actual and threshold labor cost.

Conclusions

Previous studies of Florida sugarcane production, which compared the cost and returns from mechanically harvested operations with those of hand cutting operations (Zepp and Clayton 1975, Zepp 1975, Walker 1972), found the cost advantage of the former as early as 1972-3 season. Although this cost advantage is offset by reduced revenue due to large field losses and higher trash content with mechanical harvesting for 1972-3 season, projected 1974-75 machinery operating rates and additional 10% labor cost

increase would have been sufficient to give the net returns advantage to the mechanical operation (Zepp 1975). However, the historical fact shows that the large scale mechanization investment did not happen until mid- and late 1980s, as long as 15 years from 1972-3 season. Using the data provided by these authors, the current study analyzes the dynamic decision making process of farmers with the two methodologies: net present value (NPV) approach and real options approach (ROA).

The NPV approach supports the views of previous research: NPV less initial investment cost of mechanization (\$319,815) exceeds the NPV for operation with hand cut harvesting (\$181,014), suggesting that the model farmer should have switched to mechanized operation even in 72-3 season. Then again, the methodology fails to explain the fact that only 15% of sugarcane was harvested by machine for 1972-3 season. The conclusion from the ROA is exactly opposite to that from the NPV approach. Since the sugarcane farmers in Florida are exposed to highly volatile FCF (volatility of annual rate of return = 1.7734), the value of keeping the flexibility option alive is very high, enough to overturn the NPV conclusion. Our calculation shows that the option value of investment opportunity is \$176,166. As a result, NPV less investment cost and option value is \$80,219 which is lower than NPV for the manual operation (\$181,014).

Threshold level analysis shows for the immediate investment it takes more than a 52% increase in the labor cost for both operations. This indicates that there was a rather large margin between the actual and threshold level, and the ROA explains the historical fact that large scale mechanization did not happen for as long as 15 years from 72-3 season. This ROA result at least suggests that, even when the new

technology is available and it provides the NPV advantage over the current technology, it may take a long time for it to be adopted.

While these results apply specifically to the sugar cane experience in Florida, they are suggestive of the potential for large scale mechanization of other crops such as citrus. A key finding in the sugar cane case was that the high volatility of the returns, or free cash flow (FCF), from sugar cane was a major deterrent to investment and adoption: it increased the value of maintaining the flexibility option for investment in the future rather than investing immediately and killing the option of future investment. Interestingly, the price of Florida oranges has increased greatly in the last few years ranging from \$2.89 per box in the 2003-04 season to \$9.18 per box in the 2006-07 season, an increase of more than three-fold over a four year period (USDA 2008). In no other case for the past 20 years has there been a price change greater than 1.76 times over a four year period. Whether this results in either a higher level of returns and FCF for oranges or a change in the volatility of returns is unknown at this point in time. However, either an increase in the level of returns or in the volatility of returns would alter the option value for mechanization investment. The evaluation of the flexibility option for Florida citrus and its potential effect on the extent and speed of mechanization is a subject for additional research.

References

ARMS, Economic Research Service, U.S. Department of Agriculture, Washington, DC.
<http://www.ers.usda.gov/Data/ARMS/app/Farm.aspx>.

Brockwell, J. B. and R. A. Davis. *Time Series: Theory and Methods*. Springer-Verlag (1991).

Brockwell, J. B. and R. A. Davis. *Introduction to Time Series and Forecasting*. Springer-Verlag (2002).

Carey J. M. and D. Zilberman, "A Model of Investment under Uncertainty: Modern Irrigation Technology and Emerging Markets in Water," *American Journal of Agricultural Economics*, 84(1) (2002): 171-83.

Copeland, T. and V. Antikarov. *Real Options: A Practitioner's Guide*. Texere (2003).

Copeland, T., T. Koller, and J. Murrin. *Valuation: Measuring and Managing the Value of Companies*. John Wiley and Sons (1994).

Dixit, A.K., and R.S. Pindyck. *Investment under Uncertainty*. Princeton University Press (1994).

Emerson, R.D. "Agricultural Labor Markets and Immigration." *Choices*. 22(1), 1st Qtr, 2007.

Engel, P. D. and J. Hyde "A Real Options Analysis of Automatic Milking Systems," *Agricultural and Resource Economics Review*, 32(2) (2003): 282-94.

Florida Agricultural Statistics. *Field Crops Summary*. NASS, U.S. Department of Agriculture, (various years).

Internal Revenue Service. *Statistics of Income – 2004*. Corporate Income Tax Returns, Washington, DC. (2007).

Iwai, N., R. D. Emerson, and L. M. Walters. "Legal Status and U.S. Farm Wages." Southern Agricultural Economics Association Annual Meeting, Orlando, Florida, (February 2006).

Ise, S. and J.M. Perloff. "Legal Status and Earnings of Agricultural Workers," *American Journal of Agricultural Economics*, 77 (1995): 375-86.

Kijima, M. *Introduction to Financial Engineering II: Theory of Derivatives Pricing*. Nikkagiren (1994).

Kobayashi, Y. *Derivatives and Real Option*. Chuo Keizai Sha (2003).

Napasintuwong, O. and R.D. Emerson. "Labor Substitutability in Labor Intensive Agriculture and Technological Change in the Presence of Foreign Labor," Selected Paper, American Agricultural Economics Association Annual Meeting, Denver, Colorado (August 2004).

Roka, Fritz. Dollar\$ and Cents of Mechanical Harvesting. University of Florida, IFAS. Citrus Mechanical Harvesting.
http://citrusmh.ifas.ufl.edu/pdf/economics/dollars_cents.pdf.

Samuelson, P. "Proof that Properly Anticipated Prices Fluctuate Randomly," *Industrial Management Review* 6(2) (1965): 41-9.

Taylor, J.E. "Earnings and Mobility of Legal and Illegal Immigrant Workers in Agriculture," *American Journal of Agricultural Economics*, 74 (1992): 889-96.

Trigeorgis, L. *Real Options: Managerial Flexibility and Strategy in Resource Allocation*. MIT Press (1996).

University of Florida. IFAS. Citrus Mechanical Harvesting.
<http://citrusmh.ifas.ufl.edu/index.asp?s=2&p=2>.

U.S. Department of Agriculture. Citrus Summary. Florida Agricultural Statistics Service. Orlando, FL. 1986, 2008.

U.S. Department of Agriculture. Florida Sugarcane Production Costs. Administrative Records. Washington, DC.

U.S. Department of Labor. Florida Sugarcane Labor Costs. Administrative Records. Washington, DC.

U.S. Department of Labor. Annual Reports. OWS, ETA. Washington, DC. (various years).

Walker, C. *Cost and Returns from Sugarcane in South Florida*. University of Florida Cooperative Extension Service Cir. 374 (1972).

Zepp, G.A. and J.E. Clayton. *A Comparison of Costs and Returns for Hand Cutting and Mechanically Harvesting Sugarcane in Florida, 1972-73 Season*. Food and Resource Economics Dept., University of Florida (1975).

Zepp, G.A. *Effects of Harvest Mechanization on the Demand for Labor in Florida Sugarcane Industry*. Food and Resource Economics Dept., University of Florida (1975).